Data Fitting Functions

Data Fitting functions in Intel[®] MKL provide spline-based interpolation capabilities that you can use to approximate functions, function derivatives or integrals, and perform cell search operations.

The Data Fitting component is task based. The task is a data structure or descriptor that holds the parameters related to a specific Data Fitting operation. You can modify the task parameters using the task editing functionality of the library.

For definition of the implemented operations, see Mathematical Conventions.

Data Fitting routines use the following workflow to process a task:

- 1. Create a task or multiple tasks.
- 2. Modify the task parameters.
- **3.** Perform a Data Fitting computation.
- 4. Destroy the task or tasks.

All Data Fitting functions fall into the following categories:

Task Creation and Initialization Routines - routines that create a new Data Fitting task descriptor and initialize the most common parameters, such as partition of the interpolation interval, values of the vector-valued function, and the parameters describing their structure.

Task Editors - routines that set or modify parameters in an existing Data Fitting task.

Computational Routines - routines that perform Data Fitting computations, such as construction of a spline, interpolation, computation of derivatives and integrals, and search.

Task Destructors - routines that delete Data Fitting task descriptors and deallocate resources.

You can access the Data Fitting routines through the Fortran and C89/C99 language interfaces. You can also use the C89 interface with more recent versions of C/C++, or the Fortran 90 interface with programs written in Fortran 95

The MKL/include directory of the Intel[®] MKL contains the following Data Fitting header files:

- C/C++: mkl df.h
- Fortran: mkl df.f90 and mkl df.f77

You can find examples that demonstrate C/C++ and Fortran usage of Data Fitting routines in the MKL/ examples/datafittingc and MKL/examples/datafittingf directories, respectively.

Naming Conventions

The Fortran interfaces of the Data Fitting functions are in lowercase, while the names of the types and constants are in uppercase.

The C/C++ interface of the Data Fitting functions, types, and constants are case-sensitive and can be in lowercase, uppercase, and mixed case.

The names of all routines have the following structure:

df[datatype]<base_name>

where

- df is a prefix indicating that the routine belongs to the Data Fitting component of Intel MKL.
- [datatype] field specifies the type of the input and/or output data and can be s (for the single precision real type), d (for the double precision real type), or i (for the integer type). This field is omitted in the names of the routines that are not data type dependent.
- <base_name> field specifies the functionality the routine performs. For example, this field can be NewTask1D, Interpolate1D, or DeleteTask.

Data Types

The Data Fitting component provides routines for processing single and double precision real data types. The results of cell search operations are returned as a generic integer data type.

All Data Fitting routines use the following data type:

Туре

Data Object

Fortran: TYPE (DF TASK)

Pointer to a task

C: DFTaskPtr

NOTE

The actual size of the generic integer type is platform-dependent. Before compiling your application, you need to set an appropriate byte size for integers. For details, see section *Using the ILP64 Interface vs. LP64 Interface* of the Intel[®] MKL User's Guide.

Mathematical Conventions

This section explains the notation used for Data Fitting function descriptions. Spline notations are based on the terminology and definitions of [deBoor2001]. The Subbotin quadratic spline definition follows the conventions of [StechSub76]. The quasi-uniform partition definition is based on [Schumacher2007]

Mathematical Notation in the Data Fitting Compo Concept	Denent Mathematical Notation
Partition of interpolation interval $[a, b]$, where	${x_i}_{i=1,,n}$, where $a = x_1 < x_2 < < x_n = b$
 x_i denotes breakpoints. [x_i, x_{i+1}) denotes a sub-interval (cell) of size Δ_i=x_{i+1}-x_i. 	
Quasi-uniform partition of interpolation interval [<i>a</i> , <i>b</i>]	Partition $\{x_i\}_{i=1,,n}$ which meets the constraint with a constant <i>C</i> defined as
	$1 \leq M/m \leq C$,
	where
	• $M = \max_{i=1,,n-1} (\Delta_i)$ • $m = \min_{i=1,,n-1} (\Delta_i)$ • $\Delta_i = x_{i+1} - x_i$
Vector-valued function of dimension p being fit	$f(x) = (f_1(x),, f_p(x))$
Piecewise polynomial (PP) function f of order $k+1$	$f(x) = P_i(x)$, if $x \in [x_i, x_{i+1})$, $i = 1,, n-1$
	where
	 {x_i}_{i=1,,n} is a strictly increasing sequence of breakpoints.
	• $P_i(x) = c_{i,0} + c_{i,1}(x - x_i) + \dots + c_{i,k}(x - x_i)^k$ is a polynomial of degree k (order $k+1$) over the interval $x \in [x_i, x_{i+1}]$.
Function p agrees with function g at the points $\{x_i\}_{i=1,,n}$.	For every point ζ in sequence $\{x_i\}_{i=1,,n}$ that occurs m times, the equality $p^{(i-1)}(\zeta) = g^{(i-1)}(\zeta)$ holds for all $i = 1,,m$, where $p^{(i)}(t)$ is the derivative of the <i>i</i> -th order

order.

Concept		Mathematical Notation
The <i>k</i> -th divided difference of function <i>g</i> at points $x_i,, x_{i+k}$. This difference is the leading coefficient of the polynomial of order <i>k</i> +1 that agrees with <i>g</i> at $x_i,, x_{i+k}$.		$[x_{i},, x_{i+k}] g$ In particular, • $[x_1]g = g(x_1)$ • $[x_1, x_2] g = (g(x_1) - g(x_2)) / (x_1 - x_2)$
A <i>k</i> -order derivative of interpolant $f(x)$ interpolation site τ .	<) at	$f^{(k)}(\tau)$
nterpolants to the Function g at x		
Concept	Mathematical	Notation
Linear interpolant	$P_{i}(x) = c_{1, i} + where$ • $x \in [x_{i}, x_{i+1}]$ • $c_{1, i} = g(x_{i})$ • $c_{2, i} = [x_{i}, x_{i+1}]$ • $i = 1,, n$	(x_{i+1})
Piecewise parabolic interpolant	,	$g(x_{i+1})$
	where parame continuously $P_{i-1}^{(1)}(x_i) = P_i$	
Piecewise parabolic Subbotin interpolant	where • $x \in [t_i, t_{i+1}]$ • $\{t_i\}_{i=1,,n}$ • $t_1 = x_{1,i}$ • $t_i \in (x_{i-1}]$ • $x_+ = f(x_i)$ Coefficients c_i conditions: • $P_i(x_i) = g(x_i)$	$_{+1}^{+1}$ is a sequence of knots such that
Piecewise cubic Hermite interpolant	$P_{i}(x) = c_{1,i} + where$ • $x \in [x_{i}, x_{i+1}]$ • $c_{1,i} = g(x_{i})$ • $c_{2,i} = s_{i}$ • $c_{3,i} = ([x_{i}, x_{i+1}])$	$c_{2,i}(x - x_i) + c_{3,i}(x - x_i)^2 + c_{4,i}(x - x_i)^3,$

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Concept	Mathematical Notation
	• $i = 1,, n-1$ • $s_i = g^{(1)}(x_i)$
Piecewise cubic Bessel interpolant	$P_i(x) = c_{1,i} + c_{2,i}(x - x_i) + c_{3,i}(x - x_i)^2 + c_{4,i}(x - x_i)^3,$ where
	• $x \in [x_i, x_{i+1})$ • $c_{1,i} = g(x_i)$ • $c_{2,i} = s_i$ • $c_{3,i} = ([x_i, x_{i+1}]g - s_i) / (\Delta x_i) - c_{4,i}(\Delta x_i)$ • $c_{4,i} = (s_i + s_{i+1} - 2[x_i, x_{i+1}]g) / (\Delta x_i)^2$ • $i = 1,, n-1$ • $s_i = (\Delta x_i[x_{i-1}, x_i]g + \Delta x_{i-1}[x_i, x_{i+1}]g) / (\Delta x_i + \Delta x_{i+1})$
Piecewise cubic Akima interpolant	$P_i(x) = c_{1,i} + c_{2,i}(x - x_i) + c_{3,i}(x - x_i)^2 + c_{4,i}(x - x_i)^3,$ where
	• $x \in [x_i, x_{i+1})$ • $c_{1,i} = g(x_i)$ • $c_{2,i} = s_i$ • $c_{3,i} = ([x_i, x_{i+1}]g - s_i) / (\Delta x_i) - c_{4,i}(\Delta x_i)$ • $c_{4,i} = (s_i + s_{i+1} - 2[x_i, x_{i+1}]g) / (\Delta x_i)^2$ • $i = 1,, n-1$ • $s_i = (w_{i+1}[x_{i-1}, x_i]g + w_{i-1}[x_i, x_{i+1}]g) / (w_{i+1} + w_{i-1}),$ where
Piecewise natural cubic interpolant	$w_i = [x_i, x_{i+1}]g - [x_{i-1}, x_i]g $ $P_i(x) = c_{1,i} + c_{2,i}(x - x_i) + c_{3,i}(x - x_i)^2 + c_{4,i}(x - x_i)^3,$ where
	• $x \in [x_i, x_{i+1})$ • $c_{1,i} = g(x_i)$ • $c_{2,i} = s_i$ • $c_{3,i} = ([x_i, x_{i+1}]g - s_i) / (\Delta x_i) - c_{4,i}(\Delta x_i)$ • $c_{4,i} = (s_i + s_{i+1} - 2[x_i, x_{i+1}]g) / (\Delta x_i)^2$ • $i = 1,, n-1$ • Parameter s_i depends on the condition that the interpolant is twice continuously differentiable: $P_{i-1}^{(2)}(x_i) = P_i^{(2)}(x_i)$.
Not-a-knot boundary condition.	Parameters s_1 and s_n provide $P_1 = P_2$ and $P_{n-1} = P_n$, so that the first and the last interior breakpoints are inactive.
Free-end boundary condition.	$f''(x_1) = f''(x_n) = 0$
Look-up interpolator for discrete set of points $(x_1, y_1),, (x_n, y_n)$.	$y(x) = \begin{cases} y_1, & \text{if } x = x_1 \\ y_2, & \text{if } x = x_2 \\ & \dots \\ y_n, & \text{if } x = x_n \\ error, & otherwise \end{cases}$

Concept	Mathematical Notation
Step-wise constant continuous right interpolator.	$y(x) = \begin{cases} y_1, & \text{if } x_1 \le x < x_2 \\ y_2, & \text{if } x_2 \le x < x_3 \\ & \dots \\ y_{n-1}, & \text{if } x_{n-1} \le x < x_n \\ y_n, & \text{if } x = x_n \end{cases}$
Step-wise constant continuous left interpolator.	$y(x) = \begin{cases} y_1, & \text{if } x = x_1 \\ y_2, & \text{if } x_1 < x \le x_2 \\ y_3, & \text{if } x_2 < x \le x_3 \\ & \dots \\ y_n, & \text{if } x_{n-1} < x \le x_n \end{cases}$

Data Fitting Usage Model

Consider an algorithm that uses the Data Fitting functions. Typically, such algorithms consist of four steps or stages:

1. Create a task. You can call the Data Fitting function several times to create multiple tasks.

status = dfdNewTask1D(&task, nx, x, xhint, ny, y, yhint);

2. Modify the task parameters.

```
status = dfdEditPPSpline1D( task, s_order, c_type, bc_type, bc, ic_type, ic,
scoeff, scoeffhint );
```

3. Perform Data Fitting spline-based computations. You may reiterate steps 2-3 as needed.

```
status = dfdInterpolate1D(task, estimate, method, nsite, site, sitehint, ndorder,
dorder, datahint, r, rhint, cell );
```

4. Destroy the task or tasks.

status = dfDeleteTask(&task);

See Also

Data Fitting Usage Examples

Data Fitting Usage Examples

The examples below illustrate several operations that you can perform with Data Fitting routines. If you want to run or reuse similar examples, you can get both C and Fortran source code in the .\examples \datafittingc and .\examples\datafittingf subdirectories of the Intel MKL installation directory.

The following C example demonstrates the construction of a linear spline using Data Fitting routines. The spline approximates a scalar function defined on non-uniform partition. The coefficients of the spline are returned as a one-dimensional array:

C Example of Linear Spline Construction

```
int main()
```

{

```
int status;
/* Parameters describing the partition */
MKL INT nx; /* The size of partition x */
                  /* Partition x */
double x[N];
MKL INT xhint;
                  /* Additional information about the structure of breakpoints */
/* Parameters describing the function */
MKL_INT ny; /* Function dimension */
double y[N]; /* Function values at the breakpoints */
MKL_INT yhint; /* Additional information about the function */
/* Parameters describing the spline */
MKL INT s order; /* Spline order */
MKL INT s_type;
                   /* Spline type */
MKL_INT ic_type; /* Type of internal conditions */
                   /* Array of internal conditions */
MKL INT* ic;
MKL_INT bc_type; /* Type of boundary conditions */
                  /* Array of boundary conditions */
MKL INT* bc;
MKL INT scoeffhint;
                            /* Additional information about the coefficients */
/* Initialize the partition */
nx = N;
/* Set values of partition x */
. . .
xhint = DF NO HINT; /* No additional information about the function is provided.
                         By default, the partition is non-uniform. */
/* Initialize the function */
                     /* The function is scalar. */
ny = 1;
/* Set function values */
yhint = DF NO HINT; /* No additional information about the function is provided. */
/* Create a Data Fitting task */
status = dfdNewTask1D( &task, nx, x, xhint, ny, y, yhint );
/* Check the Data Fitting operation status */
. . .
/* Initialize spline parameters */
s order = DF PP LINEAR; /* Spline is of the second order. */
s type = DF PP DEFAULT; /* Spline is of the default type. */
/* Define internal conditions for linear spline construction (none in this example) */
ic type = DF NO IC;
ic = NULL;
/* Define boundary conditions for linear spline construction (none in this example) */
bc type = DF NO BC;
bc = NULL;
scoeffhint = DF NO HINT; /* No additional information about the spline. */
/* Set spline parameters in the Data Fitting task */
status = dfdEditPPSpline1D( task, s_order, s_type, bc_type, bc, ic_type,
                          ic, scoeff, scoeffhint );
```

```
/* Check the Data Fitting operation status */
. . .
/* Use a standard computation method to construct a linear spline: */
/* P_i(x) = c_{1,i} + c_{2,i}(x - x_i), i = 0, ..., N-2 */
/* The library packs spline coefficients to array scoeff. */
/* scoeff[2*i+0]=c1,i and scoeff[2*i+1]=c2,i, i=0,..., N-2 */
status = dfdConstruct1D( task, DF PP SPLINE, DF METHOD STD );
/* Check the Data Fitting operation status */
. . .
/* Process spline coefficients */
. . .
/* Deallocate Data Fitting task resources */
status = dfDeleteTask( &task ) ;
/* Check the Data Fitting operation status */
. . .
return 0 ;
```

The following C example demonstrates cubic spline-based interpolation using Data Fitting routines. In this example, a scalar function defined on non-uniform partition is approximated by Bessel cubic spline using nota-knot boundary conditions. Once the spline is constructed, you can use the spline to compute spline values at the given sites. Computation results are packed by the Data Fitting routine in row-major format.

C Example of Cubic Spline-Based Interpolation

```
#include "mkl.h"
#define NX 100
                            /* Size of partition, number of breakpoints */
#define NSITE 1000
                            /* Number of interpolation sites */
#define SPLINE ORDER DF PP CUBIC /* A cubic spline to construct */
int main()
                  /* Status of a Data Fitting operation */
   int status;
                   /* Data Fitting operations are task based */
   DFTaskPtr task;
   /* Parameters describing the partition */
   MKL INT nx; /* The size of partition x */
                   /* Partition x */
   double x[N];
   MKL INT xhint; /* Additional information about the structure of breakpoints */
   /* Parameters describing the function */
   MKL_INT ny; /* Function dimension */
                   /* Function values at the breakpoints */
   double y[N];
   MKL INT yhint;
                   /* Additional information about the function */
   /* Parameters describing the spline */
   MKL_INT s_order; /* Spline order */
   MKL INT s_type;
                   /* Spline type */
   MKL_INT ic_type; /* Type of internal conditions */
   MKL_INT bc_type; /* Type of boundary conditions */
   MKL INT* bc; /* Array of boundary conditions */
```

```
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```

```
MKL INT scoeffhint;
                            /* Additional information about the coefficients */
/* Parameters describing interpolation computations */
MKL INT nsite; /* Number of interpolation sites */
double site[NSITE]; /* Array of interpolation sites */
MKL_INT sitehint; /* Additional information about the structure of
                      interpolation sites */
MKL INT ndorder, dorder; /* Parameters defining the type of interpolation */
double* datahint; /* Additional information on partition and interpolation sites */
MKL INT* rhint; /* Additional information on the structure of the results */
MKL INT* cell;
                 /* Array of cell indices */
/* Initialize the partition */
nx = N;
/* Set values of partition x */
xhint = DF NON UNIFORM PARTITION; /* The partition is non-uniform. */
/* Initialize the function */
ny = 1;
                    /* The function is scalar. */
/* Set function values */
. . .
yhint = DF NO HINT; /* No additional information about the function is provided. */
/* Create a Data Fitting task */
status = dfdNewTask1D( &task, nx, x, xhint, ny, y, yhint );
/* Check the Data Fitting operation status */
. . .
/* Initialize spline parameters */
s order = DF PP CUBIC; /* Spline is of the fourth order (cubic spline). */
s type = DF PP BESSEL; /* Spline is of the Bessel cubic type. */
/* Define internal conditions for cubic spline construction (none in this example) */
ic type = DF NO IC;
ic = NULL;
/* Use not-a-knot boundary conditions. In this case, the is first and the last
interior breakpoints are inactive, no additional values are provided. */
bc type = DF BC NOT A KNOT;
bc = NULL;
/* Set spline parameters in the Data Fitting task */
status = dfdEditPPSpline1D( task, s order, s type, bc type, bc, ic type,
                         ic, scoeff, scoeffhint );
/* Check the Data Fitting operation status */
. . .
/* Use a standard method to construct a cubic Bessel spline: */
/* P_i(x) = c_{1,i} + c_{2,i}(x - x_i) + c_{3,i}(x - x_i)^2 + c_{4,i}(x - x_i)^3, */
/* The library packs spline coefficients to array scoeff: */
```

```
*/
/* scoeff[4*i+0] = c<sub>1,i</sub>, scoef[4*i+1] = c<sub>2,i</sub>,
/* scoeff[4*i+2] = c<sub>3,i</sub>, scoef[4*i+1] = c<sub>4,i</sub>,
                                                       */
/* i=0,...,N-2 */
status = dfdConstruct1D( task, DF PP SPLINE, DF METHOD STD );
/* Check the Data Fitting operation status */
. . .
/* Initialize interpolation parameters */
nsite = NSITE;
/* Set site values */
. . .
sitehint = DF NON UNIFORM PARTITION; /* Partition of sites is non-uniform */
/* Request to compute spline values */
ndorder = 1;
dorder = 1;
datahint = DF NO APRIORI INFO; /* No additional information about breakpoints or
                                    sites is provided. */
rhint = DF MATRIX STORAGE ROWS; /* The library packs interpolation results
                                    in row-major format. */
cell = NULL;
                                 /* Cell indices are not required. */
/* Solve interpolation problem using the default method: compute the sline values
   at the points site(i), i=0,..., nsite-1 and place the results to array r */
status = dfdInterpolate1D( task, DF INTERP, DF METHOD STD, nsite, site,
sitehint, ndorder, &dorder, datahint, r, rhint, cell );
/* Check Data Fitting operation status */
 . . .
/* De-allocate Data Fitting task resources */
status = dfDeleteTask( &task );
/* Check Data Fitting operation status */
 . . .
return 0;
```

The following C example demonstrates how to compute indices of cells containing given sites. This example uses uniform partition presented with two boundary points. The sites are in the ascending order.

C Example of Cell Search

```
#include "mkl.h"
#define NX 100
                                /* Size of partition, number of breakpoints */
                                /* Number of interpolation sites */
#define NSITE 1000
int main()
{
                      /* Status of a Data Fitting operation */
   int status;
   DFTaskPtr task;
                      /* Data Fitting operations are task based */
   /* Parameters describing the partition */
   MKL_INT nx; /* The size of partition x */
                      /* Partition x is uniform and holds endpoints
   double x[2];
                         of interpolation interval [a, b] */
   MKL INT xhint; /* Additional information about the structure of breakpoints */
```

```
/* Parameters describing the function */
MKL_INT ny; /* Function dimension */
float *y; /* Function values at the breakpoints */
MKL_INT yhint; /* Additional information about the function
                    /* Additional information about the function */
/* Parameters describing cell search */
MKL INT nsite; /* Number of interpolation sites */
double site[NSITE]; /* Array of interpolation sites */
MKL INT sitehint; /* Additional information about the structure of sites */
MKL INT cell[NSITE]; /* Array for cell indices */
/* Initialize a uniform partition */
nx = N:
/* Set values of partition x: for uniform partition,
                                                               */
/* provide end-points of the interpolation interval [-1.0,1.0] */
x[0] = -1.0f; x[1] = 1.0f;
xhint = DF UNIFORM PARTITION; /* Partition is uniform */
/* Initialize function parameters */
/* In cell search, function values are not necessary and are set to zero/NULL values ^{\prime\prime}
ny = 0;
y = NULL;
yhint = DF NO HINT;
/* Create a Data Fitting task */
status = dfdNewTask1D( &task, nx, x, xhint, ny, y, yhint );
/* Check Data Fitting operation status */
. . .
/* Initialize interpolation (cell search) parameters */
nsite = NSITE;
/* Set sites in the ascending order */
                             /* Sites are provided in the ascending order. */
sitehint = DF SORTED DATA;
datahint = DF NO APRIORI INFO; /* No additional information
                                   about breakpoints/sites is provided.*/
/* Use a standard method to compute indices of the cells that contain
   interpolation sites. The library places the index of the cell containing
   site(i) to the cell(i), i=0,...,nsite-1 ^{\star/}
status = dfsSearchCells1D( task, DF METHOD STD, nsite, site, sitehint,
                        datahint, cell );
/* Check Data Fitting operation status */
 . . .
/* Process cell indices */
 . . .
/* Deallocate Data Fitting task resources */
status = dfDeleteTask( &task );
/* Check Data Fitting operation status */
 . . .
return 0;
```

Task Status and Error Reporting

The Data Fitting routines report a task status through integer values. Negative status values indicate errors, while positive values indicate warnings. An error can be caused by invalid parameter values or a memory allocation failure.

The status codes have symbolic names predefined in the respective header files. For the C/C++ interface, these names are defined as macros via the #define statements. For the Fortran interface, the names are defined as integer constants via the PARAMETER operators.

If no error occurred, the function returns the DF STATUS OK code defined as zero:

C/C++:	#define	OF_STATUS_OK 0			
F90/F95:	INTEGER,	PARAMETER::DF	_STATUS_	OK =	0

In case of an error, the function returns a non-zero error code that specifies the origin of the failure. Header files for both C/C++ and Fortran languages define the following status codes:

Status Codes in the Data Fitting Component

Status Code	Description		
Common Status Codes			
DF_STATUS_OK	Operation completed successfully.		
DF_ERROR_NULL_TASK	Data Fitting task is a NULL pointer.		
DF_ERROR_MEM_FAILURE	Memory allocation failure.		
DF_ERROR_METHOD_NOT_SUPPORTED	Requested method is not supported.		
DF_ERROR_COMP_TYPE_NOT_SUPPORTED	Requested computation type is not supported.		
Data Fitting Task Creation and Initialization,	, and Generic Editing Operations		
DF_ERROR_BAD_NX	Invalid number of breakpoints.		
DF_ERROR_BAD_X	Array of breakpoints is invalid.		
DF_ERROR_BAD_X_HINT	Invalid hint describing the structure of the partition.		
DF_ERROR_BAD_NY	Invalid dimension of vector-valued function y .		
DF_ERROR_BAD_Y	Array of function values is invalid.		
DF_ERROR_BAD_Y_HINT	Invalid flag describing the structure of function $_{Y}$		
Data Fitting Task-Specific Editing Operations	S		
DF_ERROR_BAD_SPLINE_ORDER	Invalid spline order.		
DF_ERROR_BAD_SPLINE_TYPE	Invalid spline type.		
DF_ERROR_BAD_IC_TYPE	Type of internal conditions used for spline construction is invalid.		
DF_ERROR_BAD_IC	Array of internal conditions for spline construction is not defined.		
DF_ERROR_BAD_BC_TYPE	Type of boundary conditions used in spline construction is invalid.		
DF_ERROR_BAD_BC	Array of boundary conditions for spline construction is not defined.		

Status Code	Description	
DF_ERROR_BAD_PP_COEFF	Array of piecewise polynomial spline coefficients is not defined.	
DF_ERROR_BAD_PP_COEFF_HINT	Invalid flag describing the structure of the piecewise polynomial spline coefficients.	
DF_ERROR_BAD_PERIODIC_VAL	Function values at the endpoints of the interpolation interval are not equal as required in periodic boundary conditions.	
DF_ERROR_BAD_DATA_ATTR	Invalid attribute of the pointer to be set or modified in Data Fitting task descriptor with the df? editidxptr task editor.	
DF_ERROR_BAD_DATA_IDX	Index of the pointer to be set or modified in the Data Fitting task descriptor with the df? editidxptr task editor is out of the pre-defined range.	
Data Fitting Computation Operations		
DF_ERROR_BAD_NSITE	Invalid number of interpolation sites.	
DF_ERROR_BAD_SITE	Array of interpolation sites is not defined.	
DF_ERROR_BAD_SITE_HINT	Invalid flag describing the structure of interpolation sites.	
DF_ERROR_BAD_NDORDER	Invalid size of the array defining derivative orders to be computed at interpolation sites.	
DF_ERROR_BAD_DORDER	Array defining derivative orders to be computed at interpolation sites is not defined.	
DF_ERROR_BAD_DATA_HINT	Invalid flag providing additional information about partition or interpolation sites.	
DF_ERROR_BAD_INTERP	Array of spline-based interpolation results is not defined.	
DF_ERROR_BAD_INTERP_HINT	Invalid flag defining the structure of spline-based interpolation results.	
DF_ERROR_BAD_CELL_IDX	Array of indices of partition cells containing interpolation sites is not defined.	
DF_ERROR_BAD_NLIM	Invalid size of arrays containing integration limits.	
DF_ERROR_BAD_LLIM	Array of the left-side integration limits is not defined.	
DF_ERROR_BAD_RLIM	Array of the right-side integration limits is not defined.	
DF_ERROR_BAD_INTEGR	Array of spline-based integration results is not defined.	
DF_ERROR_BAD_INTEGR_HINT	Invalid flag providing the structure of the array of spline-based integration results.	
DF_ERROR_BAD_LOOKUP_INTERP_SITE	Bad site provided for interpolation with look-up interpolator.	

NOTE

The routine that estimates piecewise polynomial cubic spline coefficients can return internal error codes related to the specifics of the implementation. Such error codes indicate invalid input data or other issues unrelated to Data Fitting routines.

Task Creation and Initialization Routines

Task creation and initialization routines are functions used to create a new task descriptor and initialize its parameters. The Data Fitting component provides the df?newtaskld routine that creates and initializes a new task descriptor for a one-dimensional Data Fitting task.

df?newtask1d

Creates and initializes a new task descriptor for a onedimensional Data Fitting task.

Syntax

status = dfsnewtaskld(task, nx, x, xhint, ny, y, yhint)
status = dfdnewtaskld(task, nx, x, xhint, ny, y, yhint)
status = dfsNewTasklD(&task, nx, x, xhint, ny, y, yhint)
status = dfdNewTasklD(&task, nx, x, xhint, ny, y, yhint)

Include Files

- Fortran: mkl df.f90
- C:mkl.h

Name	Туре	Description
nx	Fortran: INTEGER	Number of breakpoints representing partition of
	C: const MKL_INT	interpolation interval [a, b].
X	Fortran: REAL(KIND=4) DIMENSION(*) for dfsnewtask1d	One-dimensional array containing the sorted breakpoints from interpolation interval [a, b]. The structure of the array is defined by parameter <i>xhint</i> :
	REAL(KIND=8) DIMENSION(*) for dfdnewtaskld	 If partition is non-uniform or quasi-uniform, the array should contain nx ordered values.
	C: const float* for dfsNewTask1D	 If partition is uniform, the array should contain two entries that represent endpoints of interpolation inter [a, b].
	const double* for dfdNewTask1D	[a, b].
xhint	Fortran: INTEGER	A flag describing the structure of partition x . For the list of
	C: const MKL_INT	possible values of <i>xhint</i> , see table "Hint Values for Partition <i>x</i> ". If you set the flag to the DF_NO_HINT value, the library interprets the partition as non-uniform.
ny	Fortran: INTEGER	Dimension of vector-valued function y.

Name	Туре	Description
	C: const MKL_INT	
У	Fortran: REAL(KIND=4) DIMENSION(*) for dfsnewtask1d	Vector-valued function y , array of size nx^*ny . The storage format of function values in the array is defined by the value of flag yhint.
	REAL(KIND=8) DIMENSION(*) for dfdnewtask1d	
	C: const float* for dfsNewTask	
	const double* for dfdNewTask	
yhint	Fortran: INTEGER	A flag describing the structure of array y . Valid hint values
	C: const MKL_INT	are listed in table "Hint Values for Vector-Valued Function y ". If you set the flag to the DF_NO_HINT value, the library assumes that all ny coordinates of the vector-valued function y are provided and stored in row-major format.

Output Parameters

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.
	C: DFTaskPtr	
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the task is created successfully. Non-zero error code if the task creation failed. See "Task

Status and Error Reporting" for error code definitions.

Description

The df?newtask1d routine creates and initializes a new Data Fitting task descriptor with user-specified parameters for a one-dimensional Data Fitting task. The x and nx parameters representing the partition of interpolation interval [a, b] are mandatory. If you provide invalid values for these parameters, such as a NULL pointer x or the number of breakpoints smaller than two, the routine does not create the Data Fitting task and returns an error code.

If you provide a vector-valued function y, make sure that the function dimension ny and the array of function values y are both valid. If any of these parameters are invalid, the routine does not create the Data Fitting task and returns an error code.

If you store coordinates of the vector-valued function y in non-contiguous memory locations, you can set the yhint flag to DF_1ST_COORDINATE, and pass only the first coordinate of the function into the task creation routine. After successful creation of the Data Fitting task, you can pass the remaining coordinates using the df?editidxptr task editor.

If the routine fails to create the task descriptor, it returns a $\ensuremath{\mathtt{NULL}}$ task pointer.

The routine supports the following hint values for partition *x*:

Hint Values for Partition x

Value	Description
DF_NON_UNIFORM_PARTITION	Partition is non-uniform.
DF_QUASI_UNIFORM_PARTITION	Partition is quasi-uniform.
DF_UNIFORM_PARTITION	Partition is uniform.
DF_NO_HINT	No hint is provided. By default, partition is interpreted as non- uniform.

The routine supports the following hint values for the vector-valued function:

Hint Values for Vector-Valued Function y

Value	Description
DF_MATRIX_STORAGE_ROWS	Data is stored in row-major format according to C conventions.
DF_MATRIX_STORAGE_COLS	Data is stored in column-major format according to Fortran conventions.
DF_1ST_COORDINATE	The first coordinate of vector-valued data is provided.
DF_NO_HINT	No hint is provided. By default, the coordinates of vector-valued function y are provided and stored in row-major format.

NOTE

You must preserve the arrays x (breakpoints) and y (vector-valued functions) through the entire workflow of the Data Fitting computations for a task, as the task stores the addresses of the arrays for spline-based computations.

Task Editors

Task editors initialize or change the predefined Data Fitting task parameters. You can use task editors to initialize or modify pointers to arrays or parameter values.

Task editors can be task-specific and generic. Task-specific editors can modify more than one parameter related to a specific task. Generic editors modify a single parameter at a time.

The Data Fitting component of the Intel MKL provides the following task editors:

Data Fitting Task Editors

Editor	Description	Туре
df? editppspline1d	Changes parameters of the piecewise polynomial spline.	Task-specific
df?editptr	Changes a pointer in the task descriptor.	Generic
dfieditval	Changes a value in the task descriptor.	Generic
df?editidxptr	Changes a coordinate of data represented in matrix format. For example, a vector-valued function or spline coefficients.	Generic

df?editppspline1d

Modifies parameters representing a spline in a Data Fitting task descriptor.

Syntax

```
status = dfseditppsplineld(task, s_order, s_type, bc_type, bc, ic_type, ic, scoeff,
scoeffhint)
status = dfdeditppsplineld(task, s_order, s_type, bc_type, bc, ic_type, ic, scoeff,
scoeffhint)
status = dfsEditPPSplinelD(task, s_order, s_type, bc_type, bc, ic_type, ic, scoeff,
scoeffhint)
status = dfdEditPPSplinelD(task, s_order, s_type, bc_type, bc, ic_type, ic, scoeff,
scoeffhint)
```

Include Files

- Fortran: mkl df.f90
- C:mkl.h

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.
	C: DFTaskPtr	
s_order	Fortran: INTEGER C: const MKL_INT	Spline order. The parameter takes one of the values described in table "Spline Orders Supported by Data Fitting Functions".
s_type	Fortran: INTEGER C: const MKL_INT	Spline type. The parameter takes one of the values described in table "Spline Types Supported by Data Fitting Functions".
bc_type	Fortran: INTEGER C: const MKL_INT	Type of boundary conditions. The parameter takes one of the values described in table "Boundary Conditions Supported by Data Fitting Functions".
bc	<pre>Fortran: REAL(KIND=4) DIMENSION(*) for dfseditppspline1d REAL(KIND=8) DIMENSION(*) for dfdeditppspline1d C: const float* for dfsEditPPSpline1D const double* for dfdEditPPSpline1D</pre>	 Pointer to boundary conditions. The size of the array is defined by the value of parameter bc_type: If you set free-end or not-a-knot boundary conditions, pass the NULL pointer to this parameter. If you combine boundary conditions at the endpoints of the interpolation interval, pass an array of two elements. If you set a boundary condition for the default quadratic spline or a periodic condition for Hermite or the default cubic spline, pass an array of one element.
ic_type	Fortran: INTEGER C: const MKL_INT	Type of internal conditions. The parameter takes one of the values described in table "Internal Conditions Supported by Data Fitting Functions".

Name	Туре	Description
ic	Fortran: REAL(KIND=4) DIMENSION(*) for dfseditppspline1d	A non-NULL pointer to the array of internal conditions. The size of the array is defined by the value of parameter <i>ic_type</i> :
	<pre>REAL(KIND=8) DIMENSION(*) for dfdeditppspline1d C: const float* for dfsEditPPSpline1D const double* for dfdEditPPSpline1D</pre>	 If you set first derivatives or second derivatives internal conditions (<i>ic_type=</i>DF_IC_1ST_DER or <i>ic_type=</i>DF_IC_2ND_DER), pass an array of n-1 derivative values at the internal points of the interpolation interval. If you set the knot values internal condition for Subbotin spline (<i>ic_type=</i>DF_IC_Q_KNOT) and the knot partition is non-uniform, pass an array of n+1 elements If you set the knot values internal condition for Subbotin spline (<i>ic_type=</i>DF_IC_Q_KNOT) and the knot partition is non-uniform, pass an array of n+1 elements
scoeff	<pre>Fortran: REAL (KIND=4) DIMENSION (*) for dfseditppspline1d REAL (KIND=8) DIMENSION (*)</pre>	Spline coefficients. An array of size $s_order*(nx-1)$. The storage format of the coefficients in the array is defined by the value of flag $scoeffhint$.
	<pre>for dfdeditppspline1d C: const float* for dfsEditPPSpline1D const double* for </pre>	
scoeffhint	dfdEditPPSpline1D Fortran: INTEGER C: const MKL_INT	A flag describing the structure of the array of spline coefficients. For valid hint values, see table "Hint Values for Spline Coefficients". The library stores the coefficients in row-major format. The default value is DF_NO_HINT.
Output Paran	neters	
Name	Туре	Description

Hume	.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the routine execution completed successfully.
		 Non-zero error code if the routine execution failed. S "Task Status and Error Reporting" for error code definitions.

Description

The editor modifies parameters that describe the order, type, boundary conditions, internal conditions, and coefficients of a spline. The spline order definition is provided in the "Mathematical Conventions" section. You can set the spline order to any value supported by Data Fitting functions. The table below lists the available values:

See

Spline Orders Supported by the Data Fitting Functions

Order	Description
DF_PP_STD	Artificial value. Use this value for look-up and step- wise constant interpolants only.
DF_PP_LINEAR	Piecewise polynomial spline of the second order (linear spline).
DF_PP_QUADRATIC	Piecewise polynomial spline of the third order (quadratic spline).
DF_PP_CUBIC	Piecewise polynomial spline of the fourth order (cubic spline).

To perform computations with a spline not supported by Data Fitting routines, set the parameter defining the spline order and pass the spline coefficients to the library in the supported format. For format description, see figure "Row-major Coefficient Storage Format".

The table below lists the supported spline types:

Spline Types Supported by Data Fitting Functions

Туре	Description
DF_PP_DEFAULT	The default spline type. You can use this type with linear, quadratic, or user-defined splines.
DF_PP_SUBBOTIN	Quadratic splines based on Subbotin algorithm, [StechSub76].
DF_PP_NATURAL	Natural cubic spline.
DF_PP_HERMITE	Hermite cubic spline.
DF_PP_BESSEL	Bessel cubic spline.
DF_PP_AKIMA	Akima cubic spline.
DF_LOOKUP_INTERPOLANT	Look-up interpolant.
DF_CR_STEPWISE_CONST_INTERPOLANT	Continuous right step-wise constant interpolant.
DF_CL_STEPWISE_CONST_INTERPOLANT	Continuous left step-wise constant interpolant.

If you perform computations with look-up or step-wise constant interpolants, set the spline order to the DF PP STD value.

Construction of specific splines may require boundary or internal conditions. To compute coefficients of such splines, you should pass boundary or internal conditions to the library by specifying the type of the conditions and providing the necessary values. For splines that do not require additional conditions, such as linear splines, set condition types to DF_NO_BC and DF_NO_IC, and pass NULL pointers to the conditions. The table below defines the supported boundary conditions:

Boundary Conditions Supported by Data Fitting Functions

Boundary Condition	Description	Spline
DF_NO_BC	No boundary conditions provided.	All
DF_BC_NOT_A_KNOT	Not-a-knot boundary conditions.	Akima, Bessel, Hermite, natural cubic

Boundary Condition	Description	Spline
DF_BC_FREE_END	Free-end boundary conditions.	Akima, Bessel, Hermite, natural cubic, quadratic Subbotin
DF_BC_1ST_LEFT_DER	The first derivative at the left endpoint.	Akima, Bessel, Hermite, natural cubic, quadratic Subbotin
DF_BC_1ST_RIGHT_DER	The first derivative at the right endpoint.	Akima, Bessel, Hermite, natural cubic, quadratic Subbotin
DF_BC_2ST_LEFT_DER	The second derivative at the left endpoint.	Akima, Bessel, Hermite, natural cubic, quadratic Subbotin
DF_BC_2ND_RIGHT_DER	The second derivative at the right endpoint.	Akima, Bessel, Hermite, natural cubic, quadratic Subbotin
DF_BC_PERIODIC	Periodic boundary conditions.	Linear, all cubic splines
DF_BC_Q_VAL	Function value at point	Default quadratic
	$(x_0 + x_1)/2$	

NOTE

To construct a natural cubic spline, pass these settings to the editor:

- DF PP CUBIC as the spline order,
- DF PP NATURAL as the spline type, and
- DF BC FREE END as the boundary condition.

To construct a cubic spline with other boundary conditions, pass these settings to the editor:

- DF_PP_CUBIC as the spline order,
- DF_PP_NATURAL as the spline type, and
- the required type of boundary condition.

For Akima, Hermite, Bessel and default cubic splines use the corresponding type defined in Table Spline Types Supported by Data Fitting Functions.

You can combine the values of boundary conditions with a bitwise OR operation. This permits you to pass combinations of first and second derivatives at the endpoints of the interpolation interval into the library. To pass a first derivative at the left endpoint and a second derivative at the right endpoint, set the boundary conditions to DF BC 1ST LEFT DER OR DF BC 2ND RIGHT DER.

You should pass the combined boundary conditions as an array of two elements. The first entry of the array contains the value of the boundary condition for the left endpoint of the interpolation interval, and the second entry - for the right endpoint. Pass other boundary conditions as arrays of one element.

For the conditions defined as a combination of valid values, the library applies the following rules to identify the boundary condition type:

- If not required for spline construction, the value of boundary conditions is ignored.
- Not-a-knot condition has the highest priority. If set, other boundary conditions are ignored.
- Free-end condition has the second priority after the not-a-knot condition. If set, other boundary
 conditions are ignored.
- Periodic boundary condition has the next priority after the free-end condition.
- The first derivative has higher priority than the second derivative at the right and left endpoints.

If you set the periodic boundary condition, make sure that function values at the endpoints of the interpolation interval are identical. Otherwise, the library returns an error code. The table below specifies the values to be provided for each type of spline if the periodic boundary condition is set.

Spline Type	Periodic Boundary Condition Support	Boundary Value
Linear	Yes	Not required
Default quadratic	No	
Subbotin quadratic	No	
Natural cubic	Yes	Not required
Bessel	Yes	Not required
Akima	Yes	Not required
Hermite cubic	Yes	First derivative
Default cubic	Yes	Second derivative

Boundary Requirements for Periodic Conditions

Internal conditions supported in the Data Fitting domain that you can use for the ic_type parameter are the following:

Internal Conditions Supported by Data Fitting Functions

Internal Condition	Description	Spline
DF_NO_IC	No internal conditions provided.	
DF_IC_1ST_DER	Array of first derivatives of size n-2, where n is the number of breakpoints. Derivatives are applicable to each coordinate of the vector-valued function.	Hermite cubic
DF_IC_2ND_DER	Array of second derivatives of size $n-2$, where n is the number of breakpoints. Derivatives are applicable to each coordinate of the vector-valued function.	Default cubic
DF_IC_Q_KNOT	Knot array of size $n+1$, where n is the number of breakpoints.	Subbotin quadratic

To construct a Subbotin quadratic spline, you have three options to get the array of knots in the library:

If you do not provide the knots, the library uses the default values of knots t = {t_i}, i = 0, ..., n according to the rule:

 $t_0 = x_0, t_n = x_{n-1}, t_i = (x_i + x_{i-1})/2, i = 1, ..., n - 1.$

• If you provide the knots in an array of size n + 1, the knots form a non-uniform partition. Make sure that the knot values you provide meet the following conditions:

 $t_0 = x_0, t_n = x_{n-1}, t_i \in (x_{i-1}, x_i), i = 1, ..., n - 1.$

• If you provide the knots in an array of size 4, the knots form a uniform partition

 $t_0 = x_0, t_1 = l, t_2 = r, t_3 = x_{n-1}$, where $l \in (x_0, x_1)$ and $r \in (x_{n-2}, x_{n-1})$.

In this case, you need to set the value of the ic_{type} parameter holding the type of internal conditions to DF_IC_Q_KNOT OR DF_UNIFORM_PARTITION.

ΝΟΤΕ

Since the partition is uniform, perform an OR operation with the DF_UNIFORM_PARTITION partition hint value described in Table Hint Values for Partition x.

For computations based on look-up and step-wise constant interpolants, you can avoid calling the df? editppsplineld editor and directly call one of the routines for spline-based computation of spline values, derivatives, or integrals. For example, you can call the df?constructld routine to construct the required spline with the given attributes, such as order or type.

The memory location of the spline coefficients is defined by the *scoeff* parameter. Make sure that the size of the array is sufficient to hold s order * (*nx*-1) values.

The df?editppspline1d routine supports the following hint values for spline coefficients:

Hint Values for Spline Coefficients

Order	Description
DF_1ST_COORDINATE	The first coordinate of vector-valued data is provided.
DF_NO_HINT	No hint is provided. By default, all sets of spline coefficients are stored in row-major format.

The coefficients for all coordinates of the vector-valued function are packed in memory one by one in successive order, from function y_1 to function y_{ny} .

Within each coordinate, the library stores the coefficients as an array, in row-major format:

 $c_{1, \ 0}, \ c_{1, \ 1}, \ \ldots, \ c_{1, \ k}, \ c_{2, \ 0}, \ c_{2, \ 1}, \ \ldots, \ c_{2, \ k}, \ \ldots, \ c_{n-1, \ 0}, \ c_{n-1, \ 1}, \ \ldots, \ c_{n-1, \ k}$

Mapping of the coefficients to storage in the *scoeff* array is described below, where $c_{i,j}$ is the *j*th coefficient of the function

$$P_{i}(x) = c_{i,0} + c_{i,1}(x - x_{i}) + \dots + c_{i,k}(x - x_{i})^{k}$$

See Mathematical Conventions for more details on nomenclature and interpolants.

Row-major Coefficient Storage Format

If you store splines corresponding to different coordinates of the vector-valued function at non-contiguous memory locations, do the following:

- **1.** Set the *scoeffhint* flag to DF_1ST_COORDINATE and provide the spline for the first coordinate.
- 2. Pass the spline coefficients for the remaining coordinates into the Data Fitting task using the df? editidxptr task editor.

Using the df?editppsplineld task editor, you can provide to the Data Fitting task an already constructed spline that you want to use in computations. To ensure correct interpretation of the memory content, you should set the following parameters:

- Spline order and type, if appropriate. If the spline is not supported by the library, set the *s_type* parameter to DF PP DEFAULT.
- Pointer to the array of spline coefficients in row-major format.
- The *scoeffhint* parameter describing the structure of the array:
 - Set the *scoeffhint* flag to the DF_1ST_COORDINATE value to pass spline coefficients stored at different memory locations. In this case, you can set the parameters that describe boundary and internal conditions to zero.
 - Use the default value DF_NO_HINT for all other cases.

Before passing an already constructed spline into the library, you should call the dfieditval task editor to provide the dimension of the spline DF_NY. See table "Parameters Supported by the dfieditval Task Editor" for details.

After you provide the spline to the Data Fitting task, you can run computations that use this spline.

NOTE

You must preserve the arrays *bc* (boundary conditions), *ic* (internal conditions), and *scoeff* (spline coefficients) through the entire workflow of the Data Fitting computations for a task, as the task stores the addresses of the arrays for spline-based computations.

df?editptr

Modifies a pointer to an array held in a Data Fitting task descriptor.

Syntax

status	=	dfseditptr(<i>task</i> ,	ptr_type,	ptr)
status	=	dfdeditptr(<i>task</i> ,	ptr_type,	ptr)
status	=	dfsEditPtr(<i>task</i> ,	ptr_type,	ptr)
status	=	dfdEditPtr(<i>task</i> ,	ptr_type,	ptr)

Include Files

- Fortran: mkl_df.f90
- C:mkl.h

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.

Name	Туре	Description
	C: DFTaskPtr	
ptr_type	Fortran: INTEGER C: const MKL_INT	The parameter to change. For details, see the <i>Pointer Type</i> column in table "Pointers Supported by the df?editptr Task Editor".
ptr	Fortran: REAL (KIND=4) DIMENSION(*) for dfseditptr	New pointer. For details, see the <i>Purpose</i> column in table "Pointers Supported by the df?editptr Task Editor".
	REAL(KIND=8) DIMENSION(*) for dfdeditptr	
	C: const float* for dfsEditPtr	
	const double* for dfdEditPtr	

Output Parameters

Name	Туре	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the routine execution completed successfully.
		 Non-zero error code otherwise. See "Task Status and Error Reporting" for error code definitions.

Description

The df?editptr editor replaces the pointer of type *ptr_type* stored in a Data Fitting task descriptor with a new pointer *ptr*. The table below describes types of pointers supported by the editor:

Pointers Supported by the df?editptr Task Editor

Pointer Type	Purpose
DF_X	Partition x of the interpolation interval
DF_Y	Vector-valued function y
DF_IC	Internal conditions for spline construction. For details, see table "Internal Conditions Supported by Data Fitting Functions".
DF_BC	Boundary conditions for spline construction. For details, see table "Boundary Conditions Supported by Data Fitting Functions".
DF_PP_SCOEFF	Spline coefficients

You can use df?editptr to modify different types of pointers including pointers to the vector-valued function and spline coefficients stored in contiguous memory. Use the df?editidxptr editor if you need to modify pointers to coordinates of the vector-valued function or spline coefficients stored at non-contiguous memory locations.

If you modify a partition of the interpolation interval, then you should call the dfieditval task editor with the corresponding value of DF_XHINT, even if the structure of the partition remains the same.

If you pass a NULL pointer to the df?editptr task editor, the task remains unchanged and the routine returns an error code. For the predefined error codes, please see "Task Status and Error Reporting".

NOTE

You must preserve the arrays *x* (breakpoints), *y* (vector-valued functions), *bc* (boundary conditions), *ic* (internal conditions), and *scoeff* (spline coefficients) through the entire workflow of the Data Fitting computations which use those arrays, as the task stores the addresses of the arrays for spline-based computations.

dfieditval

Modifies a parameter value in a Data Fitting task descriptor.

Syntax

```
status = dfieditval(task, val_type, val)
status = dfiEditVal(task, val_type, val)
```

Include Files

- Fortran: mkl df.f90
- C:mkl.h

Input Parameters

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.
	C: DFTaskPtr	
val_type	Fortran: INTEGER	The parameter to change. See table "Parameters Supported
	C: const MKL_INT	by the dfieditval Task Editor".
val	Fortran: INTEGER	A new parameter value. See table "Parameters Supported by the dfieditval Task Editor".
	C: const MKL_INT	

Output Parameters

Name	Туре	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the routine execution completed successfully.
		 Non-zero error code otherwise. See "Task Status and

Error Reporting" for error code definitions.

Description

The dfieditval task editor replaces the parameter of type val_type stored in a Data Fitting task descriptor with a new value val. The table below describes valid types of parameter val_type supported by the editor:

Parameters Supported by the dfieditval Task Editor

Parameter	Purpose
DF_NX	Number of breakpoints
DF_XHINT	A flag describing the structure of partition. See table "Hint Values for Partition x " for the list of available values.
DF_NY	Dimension of the vector-valued function
DF_YHINT	A flag describing the structure of the vector-valued function. See table "Hint Values for Vector Function y " for the list of available values.
DF_SPLINE_ORDER	Spline order. See table "Spline Orders Supported by Data Fitting Functions" for the list of available values.
DF_SPLINE_TYPE	Spline type. See table "Spline Types Supported by Data Fitting Functions" for the list of available values.
DF_BC_TYPE	Type of boundary conditions used in spline construction. See table "Boundary Conditions Supported by Data Fitting Functions" for the list of available values.
DF_IC_TYPE	Type of internal conditions used in spline construction. See table "Internal Conditions Supported by Data Fitting Functions" for the list of available values.
DF_PP_COEFF_HINT	A flag describing the structure of spline coefficients. See table "Hint Values for Spline Coefficients" for the list of available values.
DF_CHECK_FLAG	A flag which controls checking of Data Fitting parameters. See table "Possible Values for the DF_CHECK_FLAG Parameter" for the list of available values.

If you pass a zero value for the parameter describing the size of the arrays that hold coefficients for a partition, a vector-valued function, or a spline, the parameter held in the Data fitting task remains unchanged and the routine returns an error code. For the predefined error codes, see "Task Status and Error Reporting".

Possible Values for the DF_CHECK_FLAG **Parameter**

Value	Description
DF_ENABLE_CHECK_FLAG	Checks the correctness of parameters of Data Fitting computational routines (default mode).
DF_DISABLE_CHECK_FLAG	Disables checking of the correctness of parameters of Data Fitting computational routines.

Use DF_CHECK_FLAG for *val_type* in order to control validation of parameters of Data Fitting computational routines such as Construct1d, Interpolate1D/InterpolateEx1d, and SearchCells1D/

SearchCellsEx1D, which can perform better with a small number of interpolation sites or integration limits (fewer than one dozen). The default mode, with checking of parameters enabled, should be used as you develop a Data Fitting-based application. After you complete development you can disable parameter checking in order to improve the performance of your application.

If you modify the parameter describing dimensions of the arrays that hold the vector-valued function or spline coefficients in contiguous memory, you should call the df?editptr task editor with the corresponding pointers to the vector-valued function or spline coefficients even when this pointer remains unchanged. Call the df?editidxptr editor if those arrays are stored in non-contiguous memory locations.

You must call the dfieditval task editor to edit the structure of the partition DF_XHINT every time you modify a partition using df?editptr, even if the structure of the partition remains the same.

df?editidxptr

Modifies a pointer to the memory representing a coordinate of the data stored in matrix format.

Syntax

status = dfseditidxptr(task, type, idx, ptr)
status = dfdeditidxptr(task, type, idx, ptr)
status = dfsEditIdxPtr(task, type, idx, ptr)
status = dfdEditIdxPtr(task, type, idx, ptr)

Include Files

- Fortran: mkl df.f90
- C:mkl.h

Input Parameters

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.
	C: DFTaskPtr	
type	Fortran: INTEGER	Type of the data to be modified. The parameter takes one of the values described in "Data Attributes Supported by
	C: const MKL_INT	the df?editidxptr Task Editor".
idx	Fortran: INTEGER	Index of the coordinate whose pointer is to be modified.
	C: const MKL_INT	
ptr	Fortran: REAL (KIND=4) DIMENSION(*) for dfseditidxptr	Pointer to the data that holds values of coordinate <i>idx</i> . For details, see table "Data Attributes Supported by the df? editidxptr Task Editor".
	REAL(KIND=8) DIMENSION(*) for dfdeditidxptr	
	C: const float* for dfsEditIdxPtr	
	const double* for dfdEditIdxPtr	

Output Parameters

Name	Туре	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the routine execution completed successfully.

Name Type

Description

• Non-zero error code otherwise. See "Task Status and Error Reporting" for error code definitions.

Description

The routine modifies a pointer to the array that holds the i dx coordinate of vector-valued function y or the pointer to the array of spline coefficients corresponding to the given coordinate.

You can use the editor if you need to pass into a Data Fitting task or modify the pointer to coordinates of the vector-valued function or spline coefficients held at non-contiguous memory locations.

Before calling this editor, make sure that you have created and initialized the task using a task creation function or a relevant editor such as the generic or specific df?editppsplineld editor.

Data Attribute	Description
DF_Y	Vector-valued function y
DF_PP_SCOEFF	Piecewise polynomial spline coefficients

When using df?editidxptr, you might receive an error code in the following cases:

- You passed an unsupported parameter value into the editor.
- The value of the index exceeds the predefined value that equals the dimension *ny* of the vector-valued function.
- You pass a NULL pointer to the editor. In this case, the task remains unchanged.

The code example below demonstrates how to use the editor for providing values of a vector-valued function stored in two non-contiguous arrays:

Computational Routines

Data Fitting computational routines are functions used to perform spline-based computations, such as:

- spline construction
- computation of values, derivatives, and integrals of the predefined order
- cell search

Once you create a Data Fitting task and initialize the required parameters, you can call computational routines as many times as necessary.

The table below lists the available computational routines:

Data Fitting Computational Routines

Routine	Description
df?construct1d	Constructs a spline for a one-dimensional Data Fitting task.
df?interpolate1d	Computes spline values and derivatives.
df?interpolateex1d	Computes spline values and derivatives by calling user-provided interpolants.
df?integrate1d	Computes spline-based integrals.
df?integrateex1d	Computes spline-based integrals by calling user- provided integrators.
df?searchcells1d	Finds indices of cells containing interpolation sites.
df?searchcellsex1d	Finds indices of cells containing interpolation sites by calling user-provided cell searchers.

If a Data Fitting computation completes successfully, the computational routines return the DF_STATUS_OK code. If an error occurs, the routines return an error code specifying the origin of the failure. Some possible errors are the following:

- The task pointer is NULL.
- Memory allocation failed.
- The computation failed for another reason.

For the list of available status codes, see "Task Status and Error Reporting".

NOTE

Data Fitting computational routines do not control errors for floating-point conditions, such as overflow, gradual underflow, or operations with Not a Number (NaN) values.

df?construct1d

Constructs a spline of the given type.

Syntax

<pre>status = dfsconstruct1d(task,</pre>	<pre>s_format, method)</pre>	
<pre>status = dfdconstruct1d(task,</pre>	s_format, method)	
<pre>status = dfsConstruct1D(task,</pre>	s_format, method)	
<pre>status = dfdConstruct1D(task,</pre>	s format, method)	

Include Files

- Fortran: mkl df.f90
- C:mkl.h

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.
	C: DFTaskPtr	

Name	Туре	Description
s_format	Fortran: INTEGER	Spline format. The supported value is DF_PP_SPLINE.
	C: const MKL_INT	
method	Fortran: INTEGER	Construction method. The supported value is
	C: const MKL_INT	DF_METHOD_STD.

Output Parameters

Name	Туре	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the routine execution completed successfully. Non-zero error code if the routine execution failed. See "Task Status and Error Reporting" for error code definitions.

Description

Before calling df?construct1d, you need to create and initialize the task, and set the parameters representing the spline. Then you can call the df?construct1d routine to construct the spline. The format of the spline is defined by parameter *s_format*. The method for spline construction is defined by parameter *method*. Upon successful construction, the spline coefficients are available in the user-provided memory location in the format you set through the Data Fitting editor. For the available storage formats, see table "Hint Values for Spline Coefficients".

df?interpolate1d/df?interpolateex1d

Runs data fitting computations.

Syntax

```
status = dfsinterpolateld(task, type, method, nsite, site, sitehint, ndorder, dorder,
datahint, r, rhint, cell)
status = dfdinterpolateld(task, type, method, nsite, site, sitehint, ndorder, dorder,
datahint, r, rhint, cell)
status = dfsinterpolateex1d(task, type, method, nsite, site, sitehint, ndorder,
dorder, datahint, r, rhint, cell, le_cb, le_params, re_cb, re_params, i_cb, i_params,
search cb, search params)
status = dfdinterpolateex1d(task, type, method, nsite, site, sitehint, ndorder,
dorder, datahint, r, rhint, cell, le cb, le params, re cb, re params, i cb, i params,
search cb, search params)
status = dfsInterpolate1D(task, type, method, nsite, site, sitehint, ndorder, dorder,
datahint, r, rhint, cell)
status = dfdInterpolate1D(task, type, method, nsite, site, sitehint, ndorder, dorder,
datahint, r, rhint, cell)
status = dfsInterpolateEx1D(task, type, method, nsite, site, sitehint, ndorder,
dorder, datahint, r, rhint, cell, le cb, le params, re cb, re params, i cb, i params,
search cb, search params)
```

status = dfdInterpolateEx1D(task, type, method, nsite, site, sitehint, ndorder, dorder, datahint, r, rhint, cell, le_cb, le_params, re_cb, re_params, i_cb, i_params, search_cb, search_params)

Include Files

- Fortran: mkl_df.f90
- C:mkl.h

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.
	C: DFTaskPtr	
type	Fortran: INTEGER	Type of spline-based computations. The parameter takes one or more values combined with an OR operation. For the
	C: const MKL_INT	list of possible values, see table "Computation Types Supported by the df?interpolate1d/ df?interpolate1d Routines".
method	Fortran: INTEGER	Computation method. The supported value is
	C: const MKL_INT	DF_METHOD_PP.
nsite	Fortran: INTEGER	Number of interpolation sites.
	C: const MKL_INT	
site	<pre>Fortran: REAL(KIND=4) DIMENSION(*) for dfsinterpolateld/ dfsinterpolateex1d REAL(KIND=8) DIMENSION(*) for dfdinterpolate1d/ dfdinterpolateex1d C: const float* for dfsInterpolate1D/ dfsInterpolateEx1D const double* for dfdInterpolate1D/</pre>	 Array of interpolation sites of size <i>nsite</i>. The structure of the array is defined by the <i>sitehint</i> parameter: If sites form a non-uniform partition, the array should contain <i>nsite</i> values. If sites form a uniform partition, the array should contain two entries that represent the left and the right interpolation sites. The first entry of the array contains the left-most interpolation point. The second entry of the array contains the right-most interpolation point.
	dfdInterpolateEx1D	
sitehint	Fortran: INTEGER	A flag describing the structure of the interpolation sites. For the list of possible values of <i>sitehint</i> , see table "Hint
	C: const MKL_INT	Values for Interpolation Sites". If you set the flag to DF_NO_HINT, the library interprets the site-defined partition as non-uniform.
ndorder	Fortran: INTEGER C: const MKL_INT	Maximal derivative order increased by one to be computed at interpolation sites.

Name	Туре	Description
dorder	<pre>Fortran: INTEGER DIMENSION(*) C: const MKL_INT*</pre>	Array of size <i>ndorder</i> that defines the order of the derivatives to be computed at the interpolation sites. If all the elements in <i>dorder</i> are zero, the library computes the spline values only. If you do not need interpolation computations, set <i>ndorder</i> to zero and pass a NULL pointer to <i>dorder</i> .
datahint	Fortran: REAL(KIND=4) DIMENSION(*) for dfsinterpolate1d/ dfsinterpolateex1d	Array that contains additional information about the structure of partition <i>x</i> and interpolation sites. This data helps to speed up the computation. If you provide a NULL pointer, the routine uses the default settings for computations. For details on the databint array see table
	REAL(KIND=8) DIMENSION(*) for dfdinterpolate1d/ dfdinterpolateex1d	computations. For details on the <i>datahint</i> array, see table "Structure of the <i>datahint</i> Array".
	C: const float* for dfsInterpolate1D/ dfsInterpolateEx1D	
	const double* for dfdInterpolate1D / dfdInterpolateEx1D	
r	Fortran: REAL(KIND=4) DIMENSION(*) for dfsinterpolate1d/ dfsinterpolateex1d	Array that contains results of computations at the interpolation sites. If you do not need spline-based interpolation or integration, set this pointer to NULL.
	REAL(KIND=8) DIMENSION(*) for dfdinterpolateld / dfdinterpolateex1d	
	C: float* for dfsInterpolate1D/ dfsInterpolateEx1D	
	double* for dfdInterpolate1D / dfdInterpolateEx1D	
rhint	Fortran: INTEGER C: const MKL_INT	A flag describing the structure of the results. For the list of possible values of <i>rhint</i> , see table "Hint Values for the <i>rhint</i> Parameter". If you set the flag to DF_NO_HINT, the library stores the result in row-major format.
cell	Fortran: INTEGER DIMENSION(*) C: MKL_INT*	Array of cell indices in partition x that contain the interpolation sites. If you do not need cell indices, set this parameter to NULL.
le_cb	Fortran: INTEGER	User-defined callback function for extrapolation at the sites to the left of the interpolation interval.
		Set to \mathtt{NULL} if you are not supplying a callback function.

Name	Туре	Description
	C: constdfsInterpCallBack for dfsInterpolateEx1D	
	constdfdInterpCallBack for dfdInterpolateEx1D	
le_params	Fortran: INTEGER DIMENSION(*)	Pointer to additional user-defined parameters passed by the library to the le_{cb} function.
	C:const void*	Set to ${\tt NULL}$ if there are no additional parameters or if you are not supplying a callback function.
re_cb	Fortran: INTEGER C:	User-defined callback function for extrapolation at the sites to the right of the interpolation interval.
	constdfsInterpCallBack for dfsInterpolateEx1D	Set to $MULL$ if you are not supplying a callback function.
	constdfdInterpCallBack for dfdInterpolateEx1D	
re_params	Fortran: INTEGER DIMENSION(*)	Pointer to additional user-defined parameters passed by the library to the re_cb function.
	C:const void*	Set to NULL if there are no additional parameters or if you are not supplying a callback function.
i_cb	Fortran: INTEGER C:	User-defined callback function for interpolation within the interpolation interval.
	constdfsInterpCallBack for dfsInterpolateEx1D	Set to $MULL$ if you are not supplying a callback function.
	constdfdInterpCallBack for dfdInterpolateEx1D	
i_params	Fortran: INTEGER DIMENSION(*)	Pointer to additional user-defined parameters passed by the library to the i_cb function.
	C:const void*	Set to NULL if there are no additional parameters or if you are not supplying a callback function.
search_cb	Fortran: INTEGER C:	User-defined callback function for computing indices of cells that can contain interpolation sites.
	constdfsSearchCellsCal lBack for dfsInterpolateEx1D	Set to NULL if you are not supplying a callback function.
	constdfdSearchCellsCal lBack for dfdInterpolateEx1D	
search_params	Fortran: INTEGER DIMENSION(*)	Pointer to additional user-defined parameters passed by the library to the <i>search_cb</i> function.
	C:const void*	Set to NULL if there are no additional parameters or if you are not supplying a callback function.

Output Parameters

Name	Туре	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the routine execution completed successfully. Non-zero error code if the routine execution failed. See "Task Status and Error Reporting" for error code definitions.

Description

The df?interpolate1d/df?interpolateex1d routine performs spline-based computations with userdefined settings. The routine supports two types of computations for interpolation sites provided in array *site*:

Computation Types Supported by the df?interpolate1d/df?interpolateex1d Routines

Туре	Description
DF_INTERP	Compute derivatives of predefined order. The derivative of the zero order is the spline value.
DF_CELL	Compute indices of cells in partition x that contain the sites.

If the sites do not belong to interpolation interval [a, b], the library uses:

- polynomial P_0 of the spline constructed on interval $[x_0, x_1]$ for computations at the sites to the left of *a*.
- polynomial P_{n-2} of the spline constructed on interval [x_{n-2}, x_{n-1}] for computations at the sites to the right of b.

Interpolation sites support the following hints:

Hint Values for Interpolation Sites

Value	Description
DF_NON_UNIFORM_PARTITION	Partition is non-uniform.
DF_UNIFORM_PARTITION	Partition is uniform.
DF_SORTED_DATA	Interpolation sites are sorted in the ascending order and define a non-uniform partition.
DF_NO_HINT	No hint is provided. By default, the partition defined by interpolation sites is interpreted as non-uniform.

NOTE

If you pass a sorted array of interpolation sites to the Intel MKL, set the *sitehint* parameter to the DF_SORTED_DATA value. The library uses this information when choosing the search algorithm and ignores any other data hints about the structure of the interpolation sites.

Data Fitting computation routines can use the following hints to speed up the computation:

- DF_UNIFORM_PARTITION describes the structure of breakpoints and the interpolation sites.
- DF_QUASI_UNIFORM PARTITION describes the structure of breakpoints.

Pass the above hints to the library when appropriate.

The *x* pointer defines the memory location for the sets of interpolation and integration results for all coordinates of function *y*. The sets are stored one by one, in the successive order of the function coordinates from y_1 to y_{ny} .

You can define the following settings for packing the results within each set:

- Computation type: interpolation, integration, or both.
- Computation parameters: derivative orders.
- Storage format for the results. You can specify the format using the *rhint* parameter values described in the table below:

Hint Values for the *rhint* Parameter

Value	Description
DF_MATRIX_STORAGE_ROWS	Data is stored in row-major format according to C conventions.
DF_MATRIX_STORAGE_COLS	Data is stored in column-major format according to Fortran conventions.
DF_NO_HINT	No hint is provided. By default, the results are stored in row- major format.

For spline-based interpolation, you should set the derivatives whose values are required for the computation. You can provide the derivatives by setting the *dorder* array of size *ndorder* as follows:

$$dorder[i] = \begin{cases} 1, if derivative of the i-th order is required \\ 0, otherwise \end{cases} i = 0, \dots, ndorder-1$$

See below a common structure of the storage formats of the interpolation results within each set r for computing derivatives of order $i_1, i_2, ..., i_m$ at *nsite* interpolation sites. In this description, j is the coordinate of the vector-valued function:

Row-major form	mat
----------------	-----

$r_j(i_1, 0)$	r _j (i ₂ , 0)	 r _j (i _m , 0)
$r_j(i_1, 1)$	$r_{j}(i_{2}, 1)$	 $r_{j}(i_{m}, 1)$
r _j (i ₁ , nsite - 1)	r _j (i ₂ , nsite - 1)	 r _j (i _m , nsite - 1)
olumn-major format		
$r_j(i_1, 0)$	$r_j(i_1, 1)$	 r _j (i ₁ , nsite - 1)
$r_{j}(i_{2}, 0)$	$r_{j}(i_{2}, 1)$	 r _j (i ₂ , nsite - 1)
r _j (i _m , 0)	r _j (i _m , 1)	 r _j (i _m , nsite - 1)

To speed up Data Fitting computations, use the *datahint* parameter that provides additional information about the structure of the partition and interpolation sites. This data represents a floating-point or a double array with the following structure:

Structure of the *datahint* Array

Element Number	Description
0	Task dimension

Element Number	Description
1	Type of additional information
2	Reserved field
3	The total number q of elements containing additional information.
4	Element (1)
q+3	Element (q)

Data Fitting computation functions support the following types of additional information for *datahint*[1]: **Types of Additional Information**

Туре	Element Number	Parameter
DF_NO_APRIORI_INFO	0	No parameters are provided. Information about the data structure is absent.
DF_APRIORI_MOST_LIKELY_CELL	1	Index of the cell that is likely to contain interpolation sites.

To compute indices of the cells that contain interpolation sites, provide the pointer to the array of size *nsite* for the results. The library supports the following scheme of cell indexing for the given partition $\{x_i\}$, i=1,...,nx:

 $\texttt{cell}[j] = i, \, \texttt{if site}[j] \in [x_i, \, x_{i+1}), \, i = 0, \dots, \, \texttt{nx},$

where

- $x_0 = -\infty$
- $x_{nx+1} = +\infty$
- *j* = 0,..., *nsite*-1

To perform interpolation computations with spline types unsupported in the Data Fitting component, use the extended version of the routine df?interpolateex1d. With this routine, you can provide user-defined callback functions for computations within, to the left of, or to the right of interpolaton interval [*a*, *b*]. The callback functions compute indices of the cells that contain the specified interpolation sites or can serve as an approximation for computing the exact indices of such cells.

If you do not pass any function for computations at the sites outside the interval [a, b], the routine uses the default settings.

See Also df?interpcallback df?searchcellscallback

df?integrate1d/df?integrateex1d

Computes a spline-based integral.

Syntax

```
status = dfsintegrate1d(task, method, nlim, llim, llimhint, rlim, rlimhint, ldatahint,
rdatahint, r, rhint)
```

```
status = dfdintegrateld(task, method, nlim, llim, llimhint, rlim, rlimhint, ldatahint,
rdatahint, r, rhint)
```

status = dfsintegrateex1d(task, method, nlim, llim, llimhint, rlim, rlimhint, ldatahint, rdatahint, r, rhint, le cb, le params, re cb, re params, i cb, i params, search cb, search params) status = dfdintegrateex1d(task, method, nlim, llim, llimhint, rlim, rlimhint, ldatahint, rdatahint, r, rhint, le_cb, le_params, re_cb, re_params, i_cb, i_params, search cb, search params) status = dfsIntegrate1D(task, method, nlim, llim, llimhint, rlim, rlimhint, ldatahint, rdatahint, r, rhint) status = dfdIntegrate1D(task, method, nlim, llim, llimhint, rlim, rlimhint, ldatahint, rdatahint, r, rhint) status = dfsIntegrateEx1D(task, method, nlim, llim, llimhint, rlim, rlimhint, ldatahint, rdatahint, r, rhint, le cb, le params, re cb, re params, i cb, i params, search cb, search params) status = dfdIntegrateEx1D(task, method, nlim, llim, llimhint, rlim, rlimhint, ldatahint, rdatahint, r, rhint, le cb, le params, re cb, re params, i cb, i params, search_cb, search params)

Include Files

- Fortran: mkl_df.f90
- C:mkl.h

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.
	C: DFTaskPtr	
method	Fortran: INTEGER	Integration method. The supported value is DF_METHOD_PP.
	C: const MKL_INT	
nlim	Fortran: INTEGER	Number of pairs of integraion limits.
	C: const MKL_INT	
llim	Fortran: REAL(KIND=4) DIMENSION(*) for dfsintegrate1d/ dfsintegrateex1d	Array of size <i>nlim</i> that defines the left-side integration limits.
	REAL(KIND=8) DIMENSION(*) for dfdintegrateld/ dfdintegrateex1d	
	C: const float* for dfsIntegrate1D/ dfsIntegrateEx1D	
	const double* for dfdIntegrate1D/ dfdIntegrateEx1D	

Name	Туре	Description
llimhint	Fortran: INTEGER	A flag describing the structure of the left-side integration
	C: const MKL_INT	limits 11im. For the list of possible values of 11imhint, see table "Hint Values for Integration Limits". If you set the flag to the DF_NO_HINT value, the library assumes that the left- side integration limits define a non-uniform partition.
rlim	Fortran: REAL(KIND=4) DIMENSION(*) for dfsintegrate1d/ dfsintegrateex1d	Array of size <i>nlim</i> that defines the right-side integration limits.
	REAL(KIND=8) DIMENSION(*) for dfdintegrate1d/ dfdintegrateex1d	
	C: const float* for dfsIntegrate1D/ dfsIntegrateEx1D	
	const double* for dfdIntegrate1D/ dfdIntegrateEx1D	
rlimhint	Fortran: INTEGER C: const MKL_INT	A flag describing the structure of the right-side integration limits <i>rlim</i> . For the list of possible values of <i>rlimhint</i> , see table "Hint Values for Integration Limits". If you set the flag to the DF_NO_HINT value, the library assumes that the right-side integration limits define a non-uniform partition.
ldatahint	Fortran: REAL(KIND=4) DIMENSION(*) for dfsintegrate1d/ dfsintegrateex1d	Array that contains additional information about the structure of partition x and left-side integration limits. For details on the <i>ldatahint</i> array, see table "Structure of the <i>datahint</i> Array" in the description of the df?
	REAL(KIND=8) DIMENSION(*) for dfdintegrate1d/ dfdintegrateex1d	Intepolate1D function.
	C: const float* for dfsIntegrate1D/ dfsIntegrateEx1D	
	const double* for dfdIntegrate1D/ dfdIntegrateEx1D	
rdatahint	<pre>Fortran: REAL(KIND=4) DIMENSION(*) for dfsintegrate1d/ dfsintegrateex1d</pre>	Array that contains additional information about the structure of partition x and right-side integration limits. For details on the <i>rdatahint</i> array, see table "Structure of the <i>datahint</i> Array" in the description of the df? Intepolate1D function.

Name	Туре	Description
	REAL(KIND=8) DIMENSION(*) for dfdintegrate1d/ dfdintegrateex1d	
	C: const float* for dfsIntegrate1D/ dfsIntegrateEx1D	
	const double* for dfdIntegrate1D/ dfdIntegrateEx1D	
r	Fortran: REAL(KIND=4) DIMENSION(*) for dfsintegrate1d/ dfsintegrateex1d	Array of integration results. The size of the array should be sufficient to hold $nlim*ny$ values, where ny is the dimension of the vector-valued function. The integration results are packed according to the settings in <i>rhint</i> .
	REAL(KIND=8) DIMENSION(*) for dfdintegrate1d/ dfdintegrateex1d	
	C: float* for dfsIntegrate1D/ dfsIntegrateEx1D	
	double* for dfdIntegrate1D / dfdIntegrateEx1D	
rhint	Fortran: INTEGER C: const MKL_INT	A flag describing the structure of the results. For the list of possible values of <i>rhint</i> , see table "Hint Values for Integration Results". If you set the flag to the DF_NO_HINT value, the library stores the results in row-major format.
le_cb	Fortran: INTEGER C:	User-defined callback function for integration on interval $[llim[i], min(rlim[i], a))$ for $llim[i] < a$.
	constdfsIntegrCallBack for dfsIntegrateEx1D	Set to $MULL$ if you are not supplying a callback function.
	constdfdIntegrCallBack for dfdIntegrateEx1D	
le_params	Fortran: INTEGER DIMENSION (*)	Pointer to additional user-defined parameters passed by the library to the le_cb function.
	C: const void*	Set to NULL if there are no additional parameters or if you are not supplying a callback function.
re_cb	Fortran: INTEGER C:	User-defined callback function for integration on interval $[max(llim[i], b), rlim[i])$ for $rlim[i] \ge b$.
	constdfsInterpCallBack for dfsIntegrateEx1D	Set to ${\tt NULL}$ if you are not supplying a callback function.

Name	Туре	Description
	constdfdInterpCallBack for dfdIntegrateEx1D	
re_params	Fortran: INTEGER DIMENSION (*)	Pointer to additional user-defined parameters passed by the library to the re_cb function.
	C:const void*	Set to NULL if there are no additional parameters or if you are not supplying a callback function.
i_cb	Fortran: INTEGER C:	User-defined callback function for integration on interval [max(a, llim[i],), min(rlim[i], b)).
	constdfsIntegrCallBack for dfsIntegrateEx1D	Set to ${\tt NULL}$ if you are not supplying a callback function.
	constdfdIntegrCallBack for dfdIntegrateEx1D	
i_params	Fortran: INTEGER DIMENSION(*)	Pointer to additional user-defined parameters passed by the library to the i_cb function.
	C:const void*	Set to NULL if there are no additional parameters or if you are not supplying a callback function.
search_cb	Fortran: INTEGER C:	User-defined callback function for computing indices of cells that can contain interpolation sites.
	constdfsSearchCellsCal lBack for dfsIntegrateEx1D	Set to ${\tt NULL}$ if you are not supplying a callback function.
	constdfdSearchCellsCal lBack for dfdIntegrateEx1D	
search_params	Fortran: INTEGER DIMENSION (*)	Pointer to additional user-defined parameters passed by the library to the <i>search_cb</i> function.
	C:const void*	Set to NULL if there are no additional parameters or if you are not supplying a callback function.

Name	Туре	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the routine execution completed successfully. Non-zero error code if the routine execution failed. See "Task Status and Error Reporting" for error code definitions.

Description

The df?integrate1d/df?integrateex1d routine computes spline-based integral on user-defined intervals

$$I(i, j) = \int_{lim[i]}^{rim[i]} f_j(x) dx, \ i = 0, \dots, nlim - 1, \ j = 0, \dots, ny - 1$$

If rlim[i] < llim[i], the routine returns</pre>

$$I(i, j) = -\int_{r\bar{a}m[i]}^{l\bar{a}m[i]} f_j(x) dx$$

The routine supports the following hint values for integration results:

Hint Values for Integration Results

Value	Description
DF_MATRIX_STORAGE_ROWS	Data is stored in row-major format according to C conventions.
DF_MATRIX_STORAGE_COLS	Data is stored in column-major format according to Fortran conventions.
DF_NO_HINT	No hint is provided. By default, the coordinates of vector-valued function γ are provided and stored in row-major format.

A common structure of the storage formats for the integration results is as follows:

Row-major format	
<i>I</i> (0, 0)	 <i>I</i> (0, nlim - 1])
I(ny - 1,0)	 <i>I</i> (<i>ny</i> - 1, <i>nlim</i> - 1])
Column-major format	
<i>I</i> (0, 0)	 I (ny - 1, 0)
<i>I</i> (0, nlim - 1])	 <i>I</i> (<i>ny</i> - 1, <i>nlim</i> - 1])

Using the *llimhint* and *rlimhint* parameters, you can provide the following hint values for integration limits:

Hint Values for Integration Limits

Value	Description
DF_SORTED_DATA	Integration limits are sorted in the ascending order and define a non-uniform partition.
DF_NON_UNIFORM_PARTITION	Partition defined by integration limits is non-uniform.
DF_UNIFORM_PARTITION	Partition defined by integration limits is uniform.
DF_NO_HINT	No hint is provided. By default, partition defined by integration limits is interpreted as non-uniform.

To compute integration with splines unsupported in the Data Fitting component, use the extended version of the routine df?integrateexld. With this routine, you can provide user-defined callback functions that compute:

- integrals within, to the left of, or to the right of the interpolation interval [a, b]
- indices of cells that contain the provided integration limits or can serve as an approximation for computing the exact indices of such cells

If you do not pass callback functions, the routine uses the default settings.

See Also

df?interpolate1d/df?interpolateex1d df?integrcallback df?searchcellscallback

df?searchcells1d/df?searchcellsex1d

Searches sub-intervals containing interpolation sites.

Syntax

```
status = dfssearchcells1d(task, method, nsite, site, sitehint, datahint, cell)
status = dfdsearchcells1d(task, method, nsite, site, sitehint, datahint, cell)
status = dfssearchcellsex1d(task, method, nsite, site, sitehint, datahint, cell,
search_cb, search_params)
status = dfdsearchcellsex1d(task, method, nsite, site, sitehint, datahint, cell,
search_cb, search_params)
status = dfsSearchCells1D(task, method, nsite, site, sitehint, datahint, cell)
status = dfdSearchCells1D(task, method, nsite, site, sitehint, datahint, cell)
status = dfsSearchCells1D(task, method, nsite, site, sitehint, datahint, cell)
status = dfsSearchCellsEx1D(task, method, nsite, site, sitehint, datahint, cell)
status = dfsSearchCellsEx1D(task, method, nsite, site, sitehint, datahint, cell,
search_cb, search_params)
```

status = dfdSearchCellsEx1D(task, method, nsite, site, sitehint, datahint, cell, search_cb, search_params)

Include Files

- Fortran: mkl_df.f90
- C:mkl.h

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task.
	C: DFTaskPtr	
method	Fortran: INTEGER	Search method. The supported value is DF_METHOD_STD.
	C: const MKL_INT	
nsite	Fortran: INTEGER	Number of interpolation sites.
	C:const MKL_INT*	
site	Fortran: REAL(KIND=4) DIMENSION(*) for	Array of interpolation sites of size <i>nsite</i> . The structure of the array is defined by the <i>sitehint</i> parameter:
	dfssearchcells1d / dfssearchcellsex1d	• If the sites form a non-uniform partition, the array should contain <i>nsite</i> values.

Name	Туре	Description
	REAL(KIND=8) DIMENSION(*) for dfdsearchcells1d/ dfdsearchcellsex1d	• If the sites form a uniform partition, the array should contain two entries that represent the left-most and the right-most interpolation sites. The first entry of the array
	C: const float* for dfsSearchCells1D/ dfsSearchCellsEx1D	contains the left-most interpolation point. The second entry of the array contains the right-most interpolation point.
	const double* for dfdSearchCells1D / dfdSearchCellsEx1D	
sitehint	Fortran: INTEGER	A flag describing the structure of the interpolation sites. For
	C: const MKL_INT	the list of possible values of <i>sitehint</i> , see table "Hint Values for Interpolation Sites". If you set the flag to DF_NO_HINT, the library interprets the site-defined partition as non-uniform.
datahint	Fortran: REAL(KIND=4) DIMENSION(*) for dfssearchcells1d/ dfssearchcellsex1d	Array that contains additional information about the structure of partition <i>x</i> and interpolation sites. This data helps to speed up the computation. If you provide a NULL pointer, the routine uses the default settings for
	REAL(KIND=8) DIMENSION(*) for dfdsearchcells1d/ dfdsearchcellsex1d	computations. For details on the <i>datahint</i> array, see table "Structure of the <i>datahint</i> Array".
	C: const float* for dfsSearchCells1D/ dfsSearchCellsEx1D	
	const double* for dfdSearchCells1D/ dfdSearchCellsEx1D	
cell	Fortran: INTEGER DIMENSION (*)	Array of cell indices in partition x that contain the interpolation sites.
	C: MKL_INT*	
search_cb	Fortran: INTEGER C:	User-defined callback function for computing indices of cells that can contain interpolation sites.
	constdfsSearchCellsCallBac k for dfsSearchCellsEx1D	Set to $MULL$ if you are not supplying a callback function.
	constdfdSearchCellsCallBac k for dfdSearchCellsEx1D	
search_pa rams	Fortran: INTEGER DIMENSION(*)	Pointer to additional user-defined parameters passed by the library to the <i>search_cb</i> function.
	C:const void*	Set to NULL if there are no additional parameters or if you are not supplying a callback function.

Name	Туре	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the routine execution completed successfully.
		 Non-zero error code if the routine execution failed. See "Task Status and Error Reporting" for error code definitions.

Description

The df?searchcells1d/df?searchcellsex1d routines return array *cell* of indices of sub-intervals (cells) in partition *x* that contain interpolation sites available in array *site*. For details on the cell indexing scheme, see the description of the df?interpolate1d/df?interpolateex1d computation routines.

Use the *datahint* parameter to provide additional information about the structure of the partition and/or interpolation sites. The definition of the *datahint* parameter is available in the description of the df? interpolate1d/df?interpolateex1d computation routines.

For description of the user-defined callback for computation of cell indices, see df?searchcellscallback.

See Also

df?interpolate1d/df?interpolateex1d df?searchcellscallback

df?interpcallback

A callback function for user-defined interpolation to be passed into df?interpolateex1d.

Syntax

status =	dfsinterpcallback(n,	cell,	site,	r,	params)
status =	dfdinterpcallback(n,	cell,	site,	r,	params)
status =	dfsInterpCallBack(n,	cell,	site,	r,	params)
status =	dfdInterpCallBack(n,	cell,	site,	r,	params)

Include Files

- Fortran: mkl df.f90
- C:mkl.h

Name	Туре	Description
п	Fortran: INTEGER(KIND=8)	Number of interpolation sites.
	C: long long*	
cell	Fortran: INTEGER(KIND=8) DIMENSION(*)	Array of size n containing indices of the cells to which the interpolation sites in array site belong.
	C: long long*	

Name	Туре	Description
site	Fortran: REAL(KIND=4) DIMENSION(*) for dfsinterpcallback	Array of interpolation sites of size <i>n</i> .
	REAL(KIND=8) DIMENSION(*) for dfdinterpcallback	
	C: float* for dfsInterpCallBack	
	double* for dfdInterpCallBack	
r	Fortran: REAL(KIND=4) DIMENSION(*) for dfsinterpcallback	Array of the computed interpolation results packed in row- major format.
	REAL(KIND=8) DIMENSION(*) for dfdinterpcallback	
	C: float* for dfsInterpCallBack	
	double* for dfdInterpCallBack	
params	Fortran: INTEGER DIMENSION(*)	Pointer to user-defined parameters of the callback function.
	C: void*	

Name	Туре	Description
status	Fortran: INTEGER	The status returned by the callback function:
	C: int	 Zero indicates successful completion of the callback operation. A negative value indicates an error. A positive value indicates a warning.

See "Task Status and Error Reporting" for error code definitions.

Description

When passed into the ${\tt df?interpolateex1d}$ routine, this function performs user-defined interpolation operation.

See Also

df?interpolate1d/df?interpolateex1d df?searchcellscallback

df?integrcallback

A callback function that you can pass into df? integrateex1d to define integration computations.

Syntax

```
status = dfsintegrcallback(n, lcell, llim, rcell, rlim, r, params)
status = dfdintegrcallback(n, lcell, llim, rcell, rlim, r, params)
status = dfsIntegrCallBack(n, lcell, llim, rcell, rlim, r, params)
status = dfdIntegrCallBack(n, lcell, llim, rcell, rlim, r, params)
```

Include Files

- Fortran: mkl df.f90
- C:mkl.h

Name	Туре	Description
п	Fortran: INTEGER(KIND=8)	Number of pairs of integration limits.
	C: long long*	
lcell	Fortran: INTEGER(KIND=8) DIMENSION(*)	Array of size <i>n</i> with indices of the cells that contain the left- side integration limits in array <i>llim</i> .
	C: long long*	
llim	Fortran: REAL(KIND=4) DIMENSION(*) for dfsintegrcallback	Array of size n that holds the left-side integration limits.
	REAL(KIND=8) DIMENSION(*) for dfdintegrcallback	
	C: float* for dfsIntegrCallBack	
	double* for dfdIntegrCallBack	
rcell	Fortran: INTEGER(KIND=8) DIMENSION(*)	Array of size <i>n</i> with indices of the cells that contain the right-side integration limits in array <i>rlim</i> .
	C: long long*	
rlim	Fortran: REAL(KIND=4) DIMENSION(*) for dfsintegrcallback	Array of size n that holds the right-side integration limits.
	REAL(KIND=8) DIMENSION(*) for dfdintegrcallback	
	C: float* for dfsIntegrCallBack	

Name	Туре	Description
	double* for dfdIntegrCallBack	
r	Fortran: REAL (KIND=4) DIMENSION(*) for dfsintegrcallback	Array of integration results. For packing the results in row- major format, follow the instructions described in df? interpolate1d/df?interpolateex1d.
	REAL(KIND=8) DIMENSION(*) for dfdintegrcallback	
	C: float* for dfsIntegrCallBack	
	double* for dfdIntegrCallBack	
params	Fortran: INTEGER DIMENSION(*)	Pointer to user-defined parameters of the callback function.
	C: void*	

Name	Туре	Description
status	Fortran: INTEGER	The status returned by the callback function:
	C: int	 Zero indicates successful completion of the callback operation. A negative value indicates an error. A positive value indicates a warning.
		See "Task Status and Error Reporting" for error code definitions.

Description

When passed into the df?integrateex1d routine, this function defines integration computations. If at least one of the integration limits is outside the interpolation interval [a, b], the library decomposes the integration into sub-intervals that belong to the extrapolation range to the left of a, the extrapolation range to the right of b, and the interpolation interval [a, b], as follows:

- If the left integration limit is to the left of the interpolation interval (*llim< a*), the df?integrateex1d routine passes *llim* as the left integration limit and min(*rlim, a*) as the right integration limit to the user-defined callback function.
- If the right integration limit is to the right of the interpolation interval (*rlim> b*), the df?integrateex1d routine passes max(*llim*, *b*) as the left integration limit and *rlim* as the right integration limit to the user-defined callback function.
- If the left and the right integration limits belong to the interpolation interval, the df?integrateex1d routine passes them to the user-defined callback function unchanged.

The value of the integral is the sum of integral values obtained on the sub-intervals.

See Also

df?integrate1d/df?integrateex1d df?integrcallback

df?searchcellscallback

df?searchcellscallback

A callback function for user-defined search to be passed into df?interpolateex1d or df? searchcellsex1d.

Syntax

<pre>status = dfssearchcellscallback(n,</pre>	site,	cell,	flag,	params)
<pre>status = dfdsearchcellscallback(n,</pre>	site,	cell,	flag,	params)
<pre>status = dfsSearchCellsCallBack(n,</pre>	site,	cell,	flag,	params)
<pre>status = dfdSearchCellsCallBack(n,</pre>	site,	cell,	flag,	params)

Include Files

- Fortran: mkl_df.f90
- C:mkl.h

Name	Туре	Description
п	Fortran: INTEGER(KIND=8)	Number of interpolation sites.
	C: long long*	
site	Fortran: REAL(KIND=4) DIMENSION(*) for dfssearchcellscallback	Array of interpolation sites of size n.
	REAL(KIND=8) DIMENSION(*) for dfdsearchcellscallback	
	C: float* for dfsSearchCellsCallBack	
	double* for dfdSearchCellsCallBack	
cell	Fortran: INTEGER(KIND=8) DIMENSION(*)	Array of size n that returns indices of the cells computed by the callback function.
	C: long long*	
flag	Fortran: INTEGER(KIND=4)	Array of size n, with values set as follows:
	DIMENSION(*)	• If the cell with index <i>cell</i> [<i>i</i>] contains <i>site</i> [<i>i</i>], set
C: int*	C: int*	 flag[i] to 1. Otherwise, set flag[i] to zero. In this case, the library interprets the index as an approximation and computes the index of the cell containing site[i] by using the provided index as a starting point for the search.
params	Fortran: INTEGER DIMENSION(*)	Pointer to user-defined parameters of the callback function.
	C: void*	

Name	Туре	Description

Name	Туре	Description
status	Fortran: INTEGER	The status returned by the callback function:
	C: int	 Zero indicates successful completion of the callback operation. A negative value indicates an error.
		 The DF_STATUS_EXACT_RESULT status indicates that cell indices returned by the callback function are exact. In this case, you do not need to initialize entries of the <i>flag</i> array.

• A positive value indicates a warning.

See "Task Status and Error Reporting" for error code definitions.

Description

When passed into the df?interpolateex1d or df?searchcellsex1d routine, this function performs a user-defined search.

See Also

df?interpolate1d/df?interpolateex1d df?interpcallback

Task Destructors

Task destructors are routines used to delete task descriptors and deallocate the corresponding memory resources. The Data Fitting task destructor dfdeletetask destroys a Data Fitting task and frees the memory.

dfdeletetask

Destroys a Data Fitting task object and frees the memory.

Syntax

```
status = dfdeletetask(task)
```

```
status = dfDeleteTask(&task)
```

Include Files

- Fortran: mkl_df.f90
- C: mkl.h

Input Parameters

Name	Туре	Description
task	Fortran: TYPE (DF_TASK)	Descriptor of the task to destroy.
	C: DFTaskPtr	
Output Pa	rameters	
Namo	Type	Description

Name	Туре	Description
status	Fortran: INTEGER	Status of the routine:
	C: int	 DF_STATUS_OK if the task is deleted successfully. Non-zero error code if the operation failed. See "Task Status and Error Reporting" for error code definitions.

Description

Given a pointer to a task descriptor, this routine deletes the Data Fitting task descriptor and frees the memory allocated for the structure. If the task is deleted successfully, the routine sets the task pointer to NULL. Otherwise, the routine returns an error code.